







- Enumerate a set S of primitives that contribute to the final surface
- Compute the arrangement A(S) by performing intersection and trimming computations
- Traverse the arrangement and extract a substructure $\delta A(S)$

































- Enumerate surface primitives
- Compute distance fields on a voxel grid
- Perform filtering operations on distance fields
- Use improved reconstruction algorithms

R Approximation Pipeline

- Enumerate surface primitives
- Compute distance fields on a voxel grid
- Perform filtering operations on distance fields
- Use improved reconstruction algorithms
 - Max-norm computations for reliable voxelization
 - Recover all connected components
 - · Faithfully reconstruct sharp features

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- Fast distance field computation
- Max-norm based voxelization
- Boundary reconstruction
- Analysis
- Applications
 - Boundary evaluation
 - Swept volume computation
 - Medial axis computation
 - Minkowski sums











Collision Detection Surface Reconstruction Robot Motion Planning Non-Photorealistic Rendering Surface Simplification Mesh Generation Shape Analysis



Approximating the Distance

- Avoid per-pixel distance evaluation
- Point-sample the distance function
- Reconstruct by rendering polygonal mesh

Line





Triangle

Point

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■ 4 -20 times speedup over HAVOC3D					
Shell Charge	4460	128x126x126	31.69	3.38	
Head	21764	79x106x128	52.47	13.60	
Bunny	69451	128x126x100	212.71	36.21	
Cassini	90879	94x128x96	1102.01	47.90	



2 - 75 times speedup

Model	Resolution	CPU (s)	GPU (s)
Shell Charge	128x126x126	3.50	0.14
Head	79x106x128	0.18	0.08
Bunny	128x126x100	0.68	0.13
Cassini	94x128x96	7.59	0.1

 Reconstruction: CPU vs. GPU Depends on grid size 2 - 75 times speedup via GPUs 				
Shell Charge	128x126x126	3.50	0.14	
Head	79x106x128	0.18	0.08	
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Markov decision processes [Tsitsiklis et al. 96, Guestrin et al. 2001]

- Discrete objects in supercover model [Andres et al. 96]
- Image analysis [Lindquist 99]
- Volume graphics [Wang & Kaufman 94, Sramek & Kaufman 99]













T	Equation Solving
0 0 0	Solve above equations for each vertex, edge and face Solution set is finite in general Obtain a set X of feasible values for the closest point Calculate min $\{ x-p _{\infty} x \in X \}$
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- Approach similar to [Hoff et al. 1999]
- Render distance function for each primitive
- Z-buffer holds the distance field



























M Sharp Features

other?

al. 03]

Surface-surface intersection causes many sharp

features on the boundary of the final surface

When do two surfaces S1 and S2 intersect each

Track the bisector surface d1-d2, where d1, d2 are the distance functions for the two surfaces [Varadhan et

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Let $\boldsymbol{S}:$ exact answer of the union or envelope computation $B(\boldsymbol{S}):$ boundary of S

Our approximation algorithm takes as input ϵ > 0, and generates an approximation $A(\epsilon)$

 $B(A(\varepsilon))$: denote the boundary of the approximation

R Bounds on Approximation

Theorem 1: Given any ϵ > 0, our algorithm computes an approximation B(A($\epsilon)$) such that

2-Hausdorff($B(A(\varepsilon)), B(S)) < \varepsilon$,

where 2-Hausdorff is the two sided Hausdorff distance

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Acknowledgements

- Army Research Office
- Intel
- National Science Foundation
- Office of Naval Research

