



# Utilizing Large-Scale Randomized Response at Google: RAPPOR and its lessons

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# RAPPOR Motivation: Hijacking of Chrome Settings

Find the Chrome homepages/search-engines used by clients  
... with privacy for each user

I.e., find popularity %'s of

Yahoo! Search, Bing, ...

Also: detect unusually high %'s for  
sites installing unwanted software

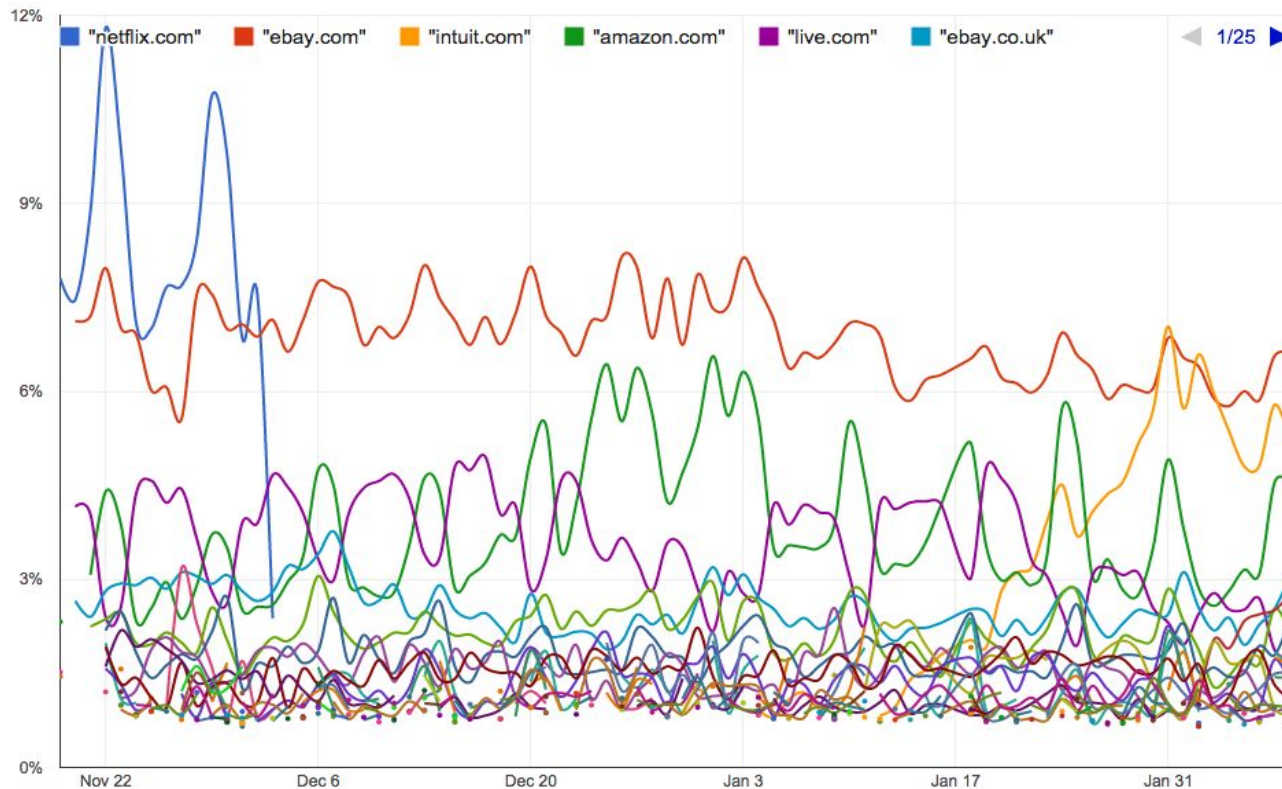
RAPPOR can find them, without  
seeing any user's homepage!



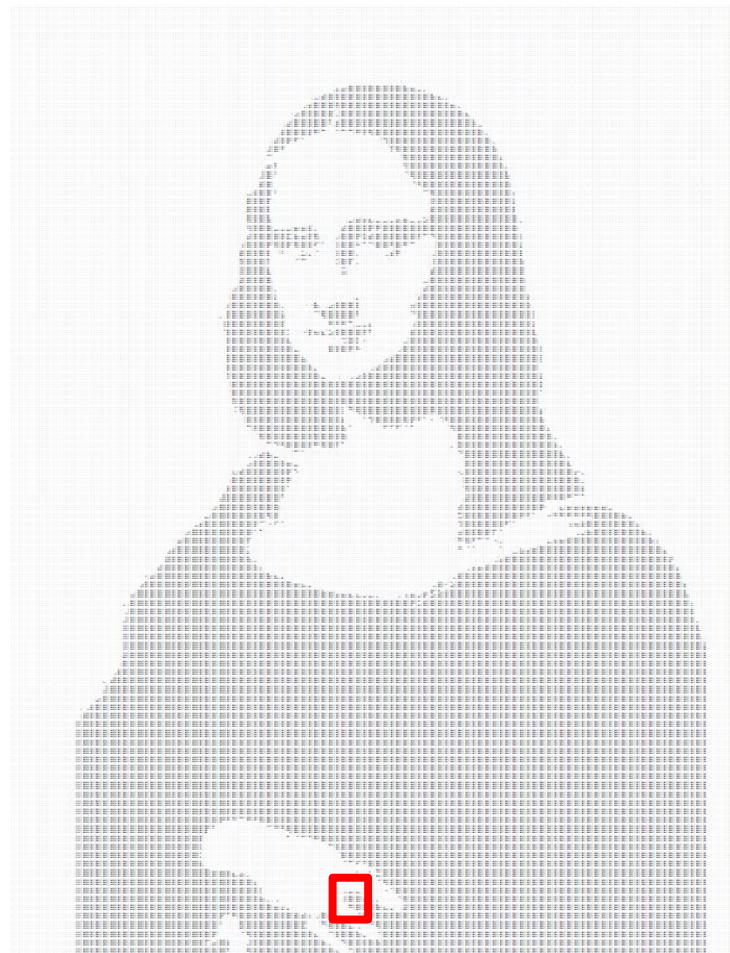
# Who on the Web is still using Silverlight?

*Estimated by  
RAPTOR*

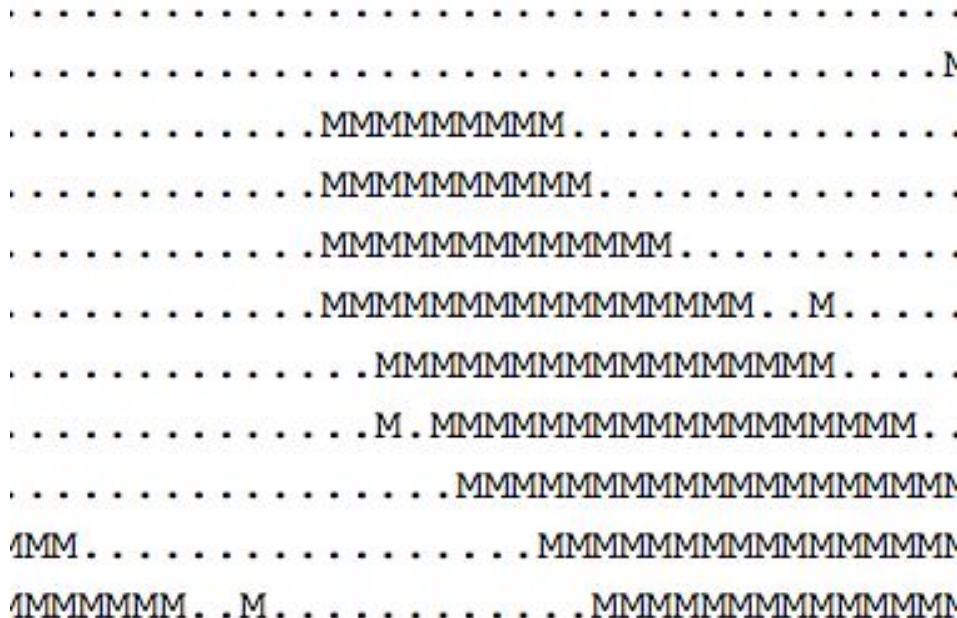
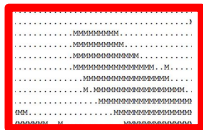
**netflix**  
**ebay**  
**intuit**  
**amazon**  
**live**



# Metaphor for RAPPOR



# Microdata: An individual's report



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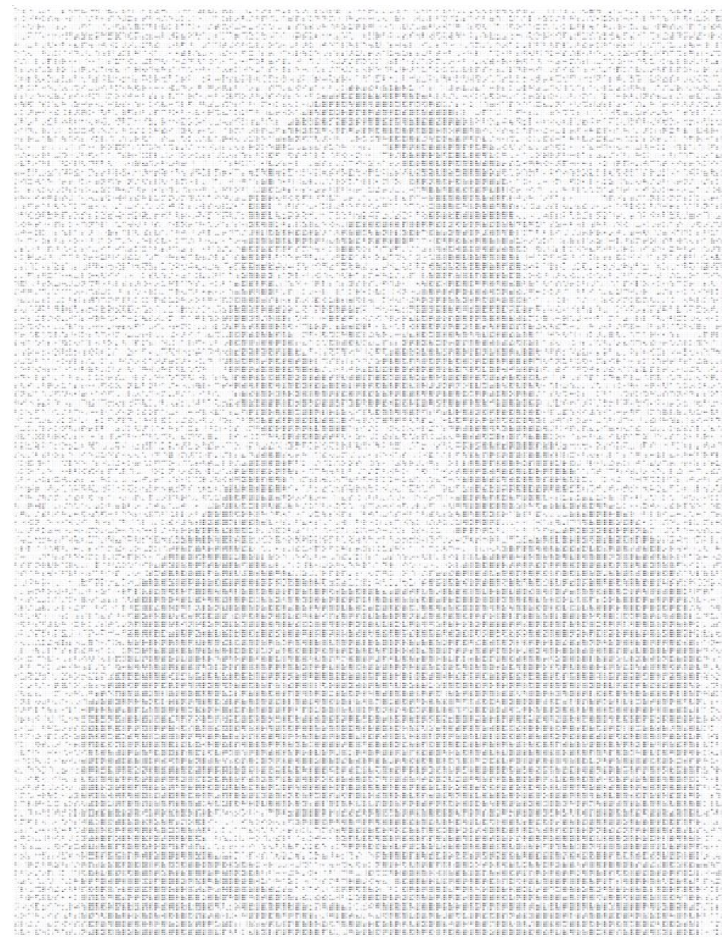
Each bit is flipped with  
probability  
25%



```
.....M.....MM.M.....MMM.M..  
.....MM...MMMM..  
...M..MM.MM..MMM.M.MM.M...M..MM..  
.MM.....MMM.....MMMMMMMMMM...M...MM  
.M...M.....MM..MMMMMMM...M..  
M.....M..MM.MMMMMMMMMMMMMMMMMM...M  
.....M.....M.M.M.MMMMMM...MMMMM..  
...M.....M.MM.M.MM..M..M..MM.MMMMM  
M...M.M.....M.M..M..MMM.MMMMM.MMMM  
.MMM.M...M.M.M.....MMMMMMMMMM.M
```



# Big picture remains!



# Best practice for learning statistics about users/clients

- **Collect** user data (perhaps with unique id for each user)
- **Scrub** IP addresses, timestamps, etc., from user data
- **Keep central database** of scrubbed data (e.g., for 2 weeks)
  - Keep only aggregates for older data
- **Report aggregates of data over a threshold** (e.g., 10 users)

Can be the best approach (e.g., for opt-in, low-sensitivity data)



# RAPPOR: Learn user statistics with much stronger privacy

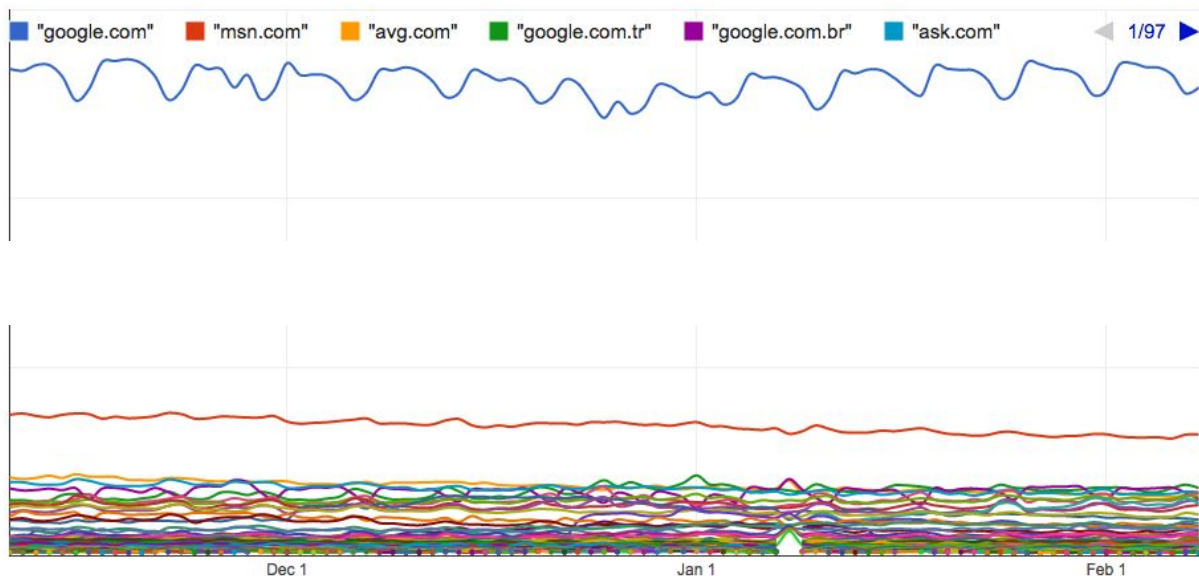
- **Rigorous and meaningful privacy guarantees** for each user
- **No central database** (hackable, subpoenaable) of user data
- User's privacy **doesn't depend on a trusted third party**
- **No privacy externalities** (e.g., from trackable user IDs)

Well-suited to sensitive user data, such as URLs from users

Dashboard at [redacted]

# Chrome homepages (over 90 days)

Estimated proportions



google

msn

avg

google tr

google br

# Gold Standard of Security

Same key aspects in software construction & computer security

<u>In programming</u>		<u>In security</u>
Specification	=	Security policy
Implementation	=	Enforcement mechanism
Correctness	=	Assurance
Methodology*	=	Security model

\* e.g., **functional** vs. **declarative** vs. **imperative programming**

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\* e.g., **HIPAA vs. usage control vs. local- or database-differential privacy**

# Takeaways from this talk

1. **Randomized response**

Learning categorical data and aggregating Bloom filters

2. **RAPPOR's 2-level randomized response**

Longitudinal differential privacy and anonymity

3. Lessons learnt from the large-scale deployment of a randomized-response privacy mechanism

4. Follow-up works

# 1. Randomized Response: Collecting a sensitive Boolean

Developed in 1960's for sensitive surveys

***“Are you now, or have you ever been, a member of the communist party?”***

- a. Flip a coin, **in private**
- b. If coin comes up heads, respond “Yes”
- c. If coin comes up tails, tell the truth

Estimate true “Yes” ratio with: “Yes”% - 50%



# 1. Randomized Response: Collecting a sensitive Boolean

Developed in 1960's for sensitive surveys

***“Are you now, or have you ever been, a member of the communist party?”***

- a. Flip a coin, **in private**
- b. If coin comes up heads,  
--- flip another coin to select randomly “Yes” or “No”
- c. If coin comes up tails, tell the truth

**Satisfies differential privacy property (with two coins)**

Still easy to estimate true “Yes” ratio

# Randomized response on categorical Boolean values

- If number of categories is small, can do an independent randomized response for each category
  - Bit-by-bit array of randomized responses

0	1	0	1	1	1	0	0	0	0	0	1	0	1	0	0	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

- Example: The categories may refer to salary ranges
  - Users do a “yes/no” randomized response for each range

0	1	0	1	1	1	0	0	0	0	0	1	0	1	0	0	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

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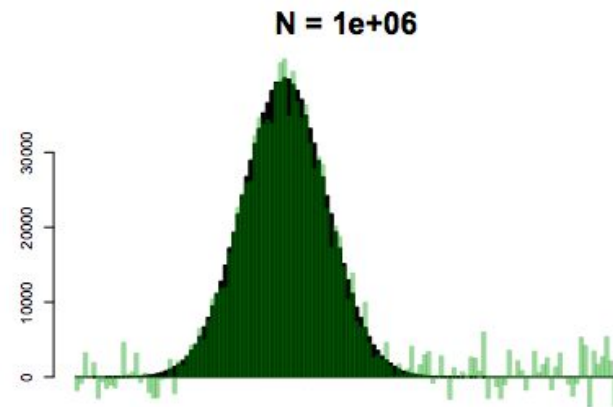
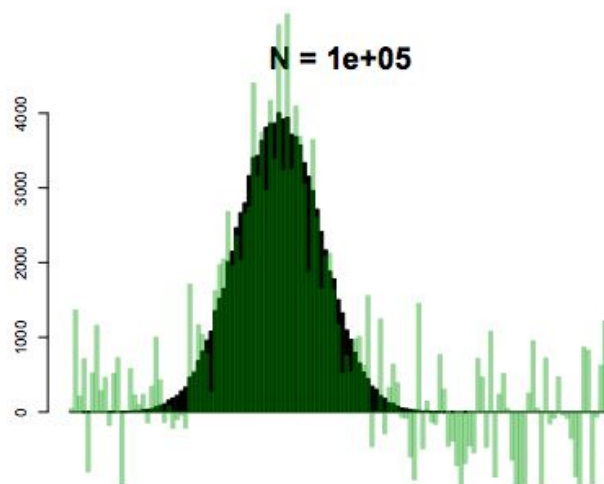
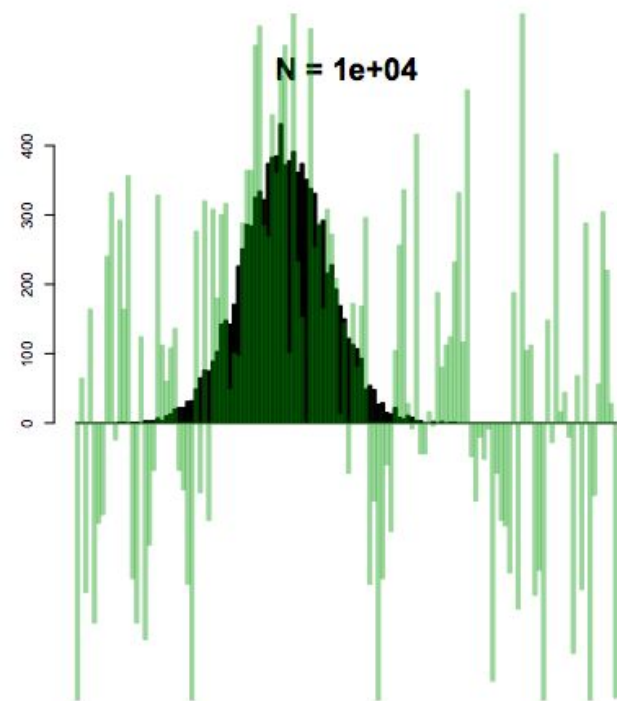
0	1	0	1	1	1	0	0	0	0	0	1	0	1	0	0	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

- Example: The categories may refer to salary ranges
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---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

This user's salary lies in this range.  
The “Yes” coin came up heads, so bit is “1”.

# Learning the shape of the Salaries distribution

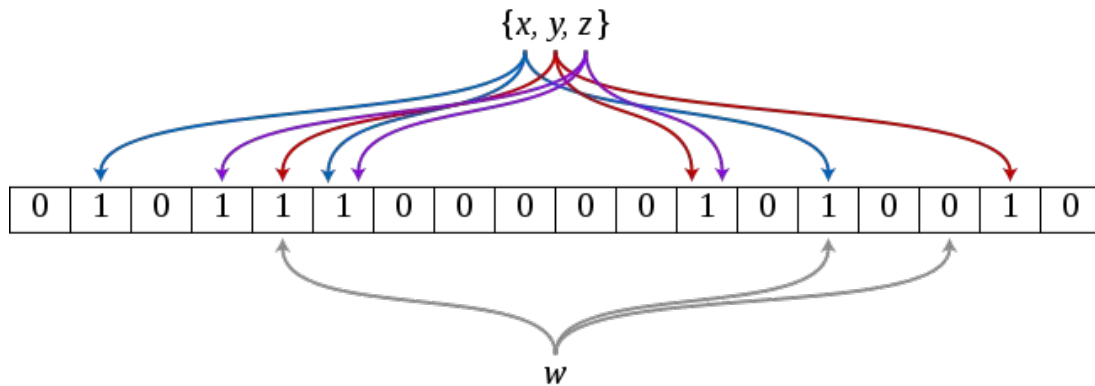


Users flip a “yes” coin for just one bit;  
“no” coins for others

No prior knowledge of the shape of the distribution.

# Bloom filters to handle large sets of categories

- Compressed representation of a large set



- To minimize collisions/false positives, use multiple cohorts
  - Randomly assign clients to one of  $m$  cohorts
  - Each cohort uses different Bloom-filter hash functions

## 2. RAPPOR two-level randomization and differential privacy

- Problem to ask the communist question repeatedly
  - Average of coin flips eventually reveals the true answer
- **Memoization** is the trick: Reuse the same answer
- But memoized random bits can hurt anonymity
  - Repeated bit sequence forms a unique tracking ID
- **Randomization of memoized response** is the answer!
  - Flip coins on a value, and memoize
  - Then report coin flips on the memoized data



# RAPPOR algorithm

1. Hash a value  $v$  into Bloom filter  $B$  using  $h$  hash functions
2. Memoize a **Permanent Randomized Response**  $B'$

$$B'_i = \begin{cases} 1, & \text{with probability } \frac{1}{2}f \\ 0, & \text{with probability } \frac{1}{2}f \\ B_i, & \text{with probability } 1 - f \end{cases}$$

3. Report an **Instantaneous Randomized Response**  $S$

$$P(S_i = 1) = \begin{cases} q, & \text{if } B'_i = 1. \\ p, & \text{if } B'_i = 0. \end{cases}$$

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$f = \frac{1}{2}$   
for example

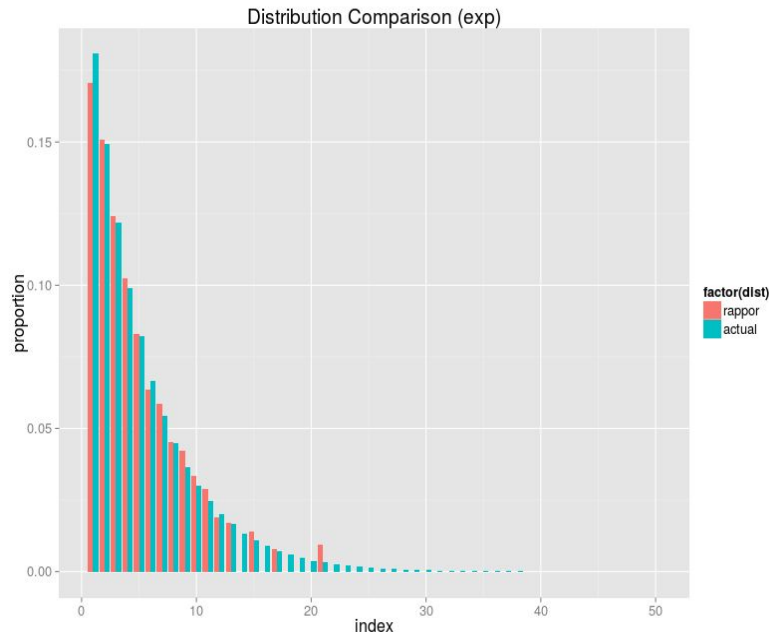
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$q = \frac{3}{4}$  and  $p = \frac{1}{2}$   
for example

# OSS project

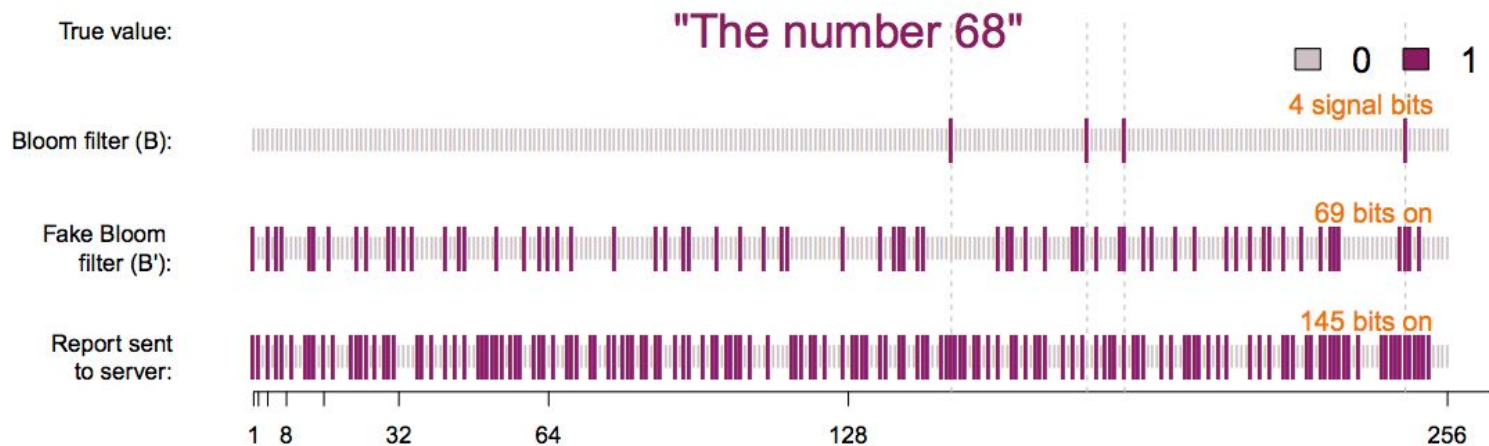
- Contents of <https://github.com/google/rappor>
  - Demo that you can run with a couple shell commands
  - Client library
  - Analysis tools and simulation
  - Documentation
  - Analysis service
  - Clients code in a few languages



# Lessons Learnt

# Design for simple explainability

Critical to get comfort / acceptance from **everybody**  
... (also need reasonable  $\epsilon$ , and may want user opt-in)

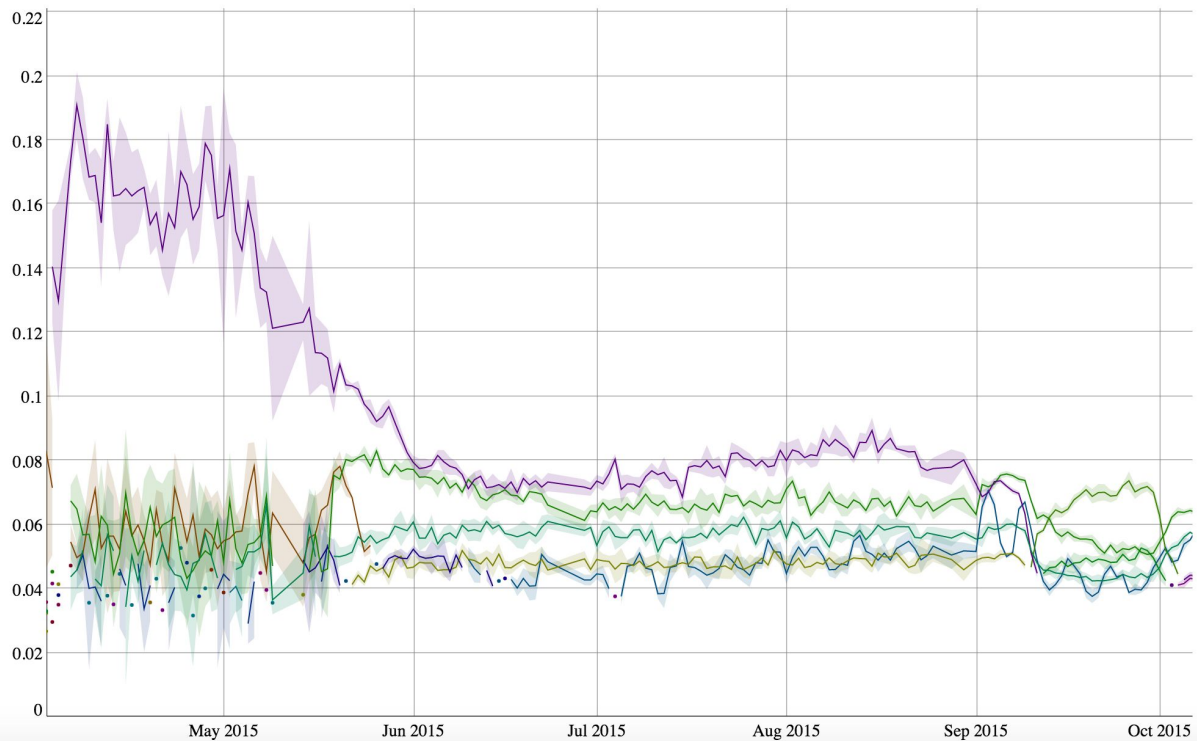


# There will be growing pains

- Transitioning from a research prototype to a real product
- Scalability
- Versioning

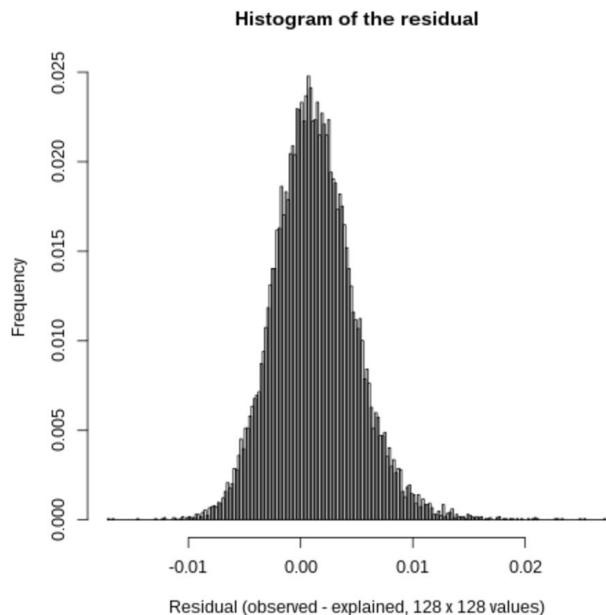


# Communicate Uncertainty

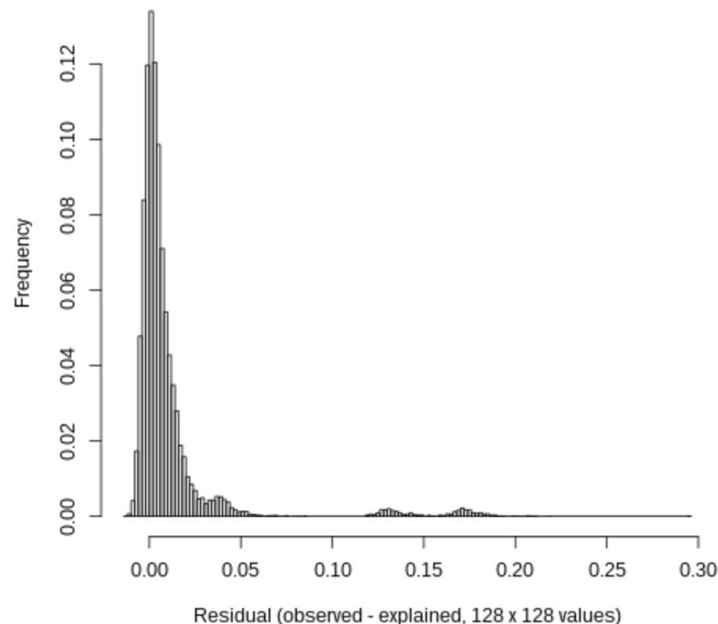


# Candidates? – Enable diagnostics on collected data

No missing candidates



Three missing candidates



# Know thy Enemies and Friends

If **raw data** is being collected:

- privacy people & technology are a hindrance to utility
  - hard to avoid the slippery slope
- ... bodes ill for (pure) database-differential privacy

If **statistical/privacy-protected data** is collected:

- privacy people become essential to utility
  - big step onto the slippery slope
- ... good reason to add noise early

# Keep your friends close ...

- Partner closely with the users, and monitor their use
  - `tools/metrics/rappor/rappor.xml` - `chromium/src`
- Avoid users treating your technology as a black box
  - they'll be disappointed & affect user privacy w/o utility
- Set and manage expectations
  - e.g., local differential privacy can only see peaky tops

# The world depends on trust; we can't do without it

- Google provides data for Chrome and RAPPOR!
- The  $\epsilon$  for RAPPOR's are just worst-case fallbacks
  - ... do much better, unless Google explicitly chooses evil
- But, without trust, those  $\epsilon$  only allow seeing peaky tops
- Need to work on better basis for combining trust with privacy
  - E.g., via technical and contractual separation of concerns
  - Backed by verifiable enforcement teeth

# Follow-up Works

- Giulia Fanti, Vasyl Pihur, Úlfar Erlingsson, “Building a RAPPOR with the Unknown: Privacy-Preserving Learning of Associations and Data Dictionaries”, PoPETS 2016
  - Two-way contingency tables and recovering missing candidates
- Bassily, Smith, “Local, Private, Efficient Protocols for Succinct Histograms,” STOC 2015
- Kairouz, Bonawitz, Ramage, “Discrete Distribution Estimation under Local Privacy”, <https://arxiv.org/abs/1602.07387>
- Qin et al., “Heavy Hitter Estimation over Set-Valued Data with Local Differential Privacy”, CCS 2016



# Follow-up Works

- Abadi, Chu, Goodfellow, McMahan, Mironov, Talwar, Zhang. “Deep learning with differential privacy.” ACM CCS 2016.
- Papernot, Abadi, Erlingsson, Goodfellow, Talwar. “Semi-supervised Knowledge Transfer for Deep Learning from Private Training Data.” ICLR 2017.

# Conclusions

RAPPOR – locally differentially-private mechanism for reporting of categorical and string data

- First Internet-scale deployment of differential privacy
- Explainable
- Conservative
- Open-sourced
- Challenging
- ... just the beginning

**Thank you!**

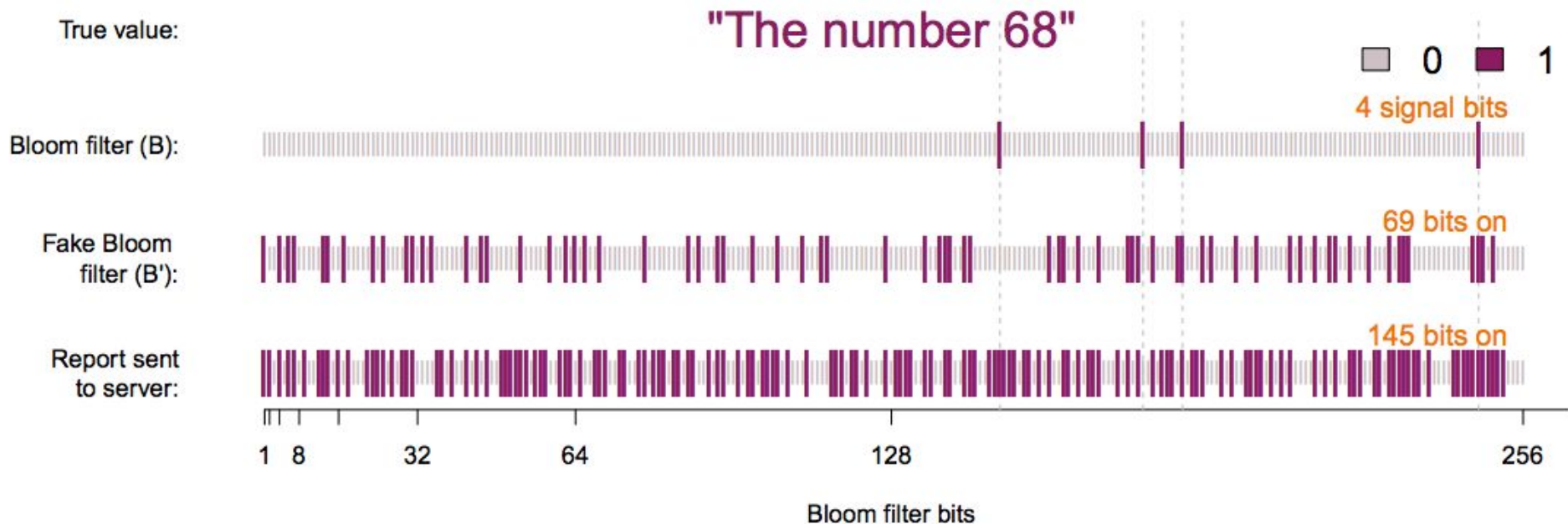
**Any questions?**

*—pseudorandom@google.com—*

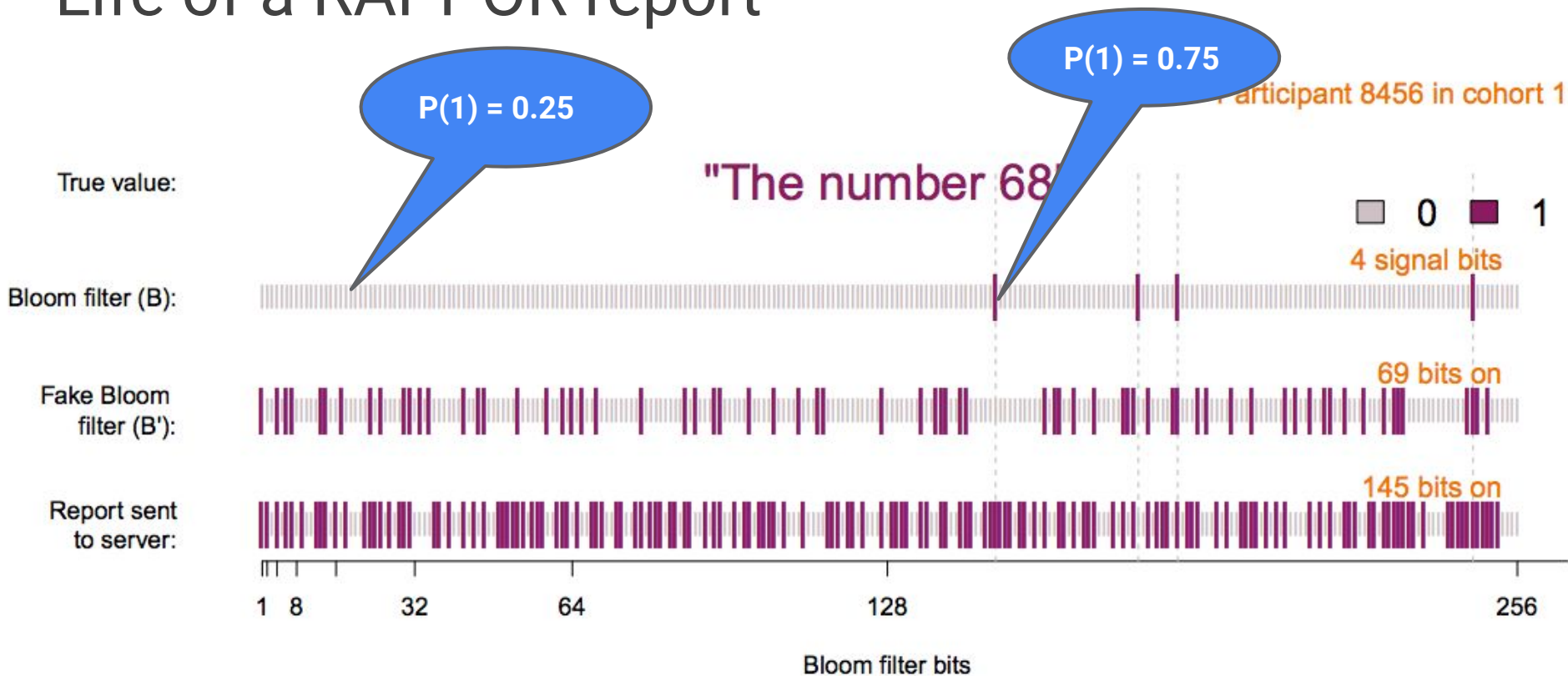
Backup

# Life of a RAPPOR report

Participant 8456 in cohort 1



# Life of a RAPPOR report



# Life of a RAPPOR report

Participant 8456 in cohort 1

"The number 68"

True value:

0 1

4 signal bits

Bloom filter (B):

Fake Bloom filter (B'):

69 bits on

Report sent to server:

145 bits on

$$P(1) = 0.50$$

$$P(1) = 0.75$$

Bloom filter bits

# Differential Privacy of RAPPOR

- **Permanent Randomized Response** satisfies differential privacy at

$$\epsilon_{\infty} = 2h \ln \left( \frac{1 - \frac{1}{2}f}{\frac{1}{2}f} \right)$$

- **Instantaneous Randomized Response** has differential privacy at

$$\epsilon_1 = h \log \left( \frac{q^*(1 - p^*)}{p^*(1 - q^*)} \right)$$



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- **Permanent Randomized Response** satisfies differential privacy at

$$\epsilon_{\infty} = 2h \ln \left( \frac{1 - \frac{1}{2}f}{\frac{1}{2}f} \right) = \mathbf{4 \ln(3)}, \text{ for example}$$

- **Instantaneous Randomized Response** has differential privacy at

$$\epsilon_1 = h \log \left( \frac{q^*(1 - p^*)}{p^*(1 - q^*)} \right) \approx \mathbf{\ln(3)}, \text{ for example}$$

# Decoding RAPPOR

True bit counts, with no noise

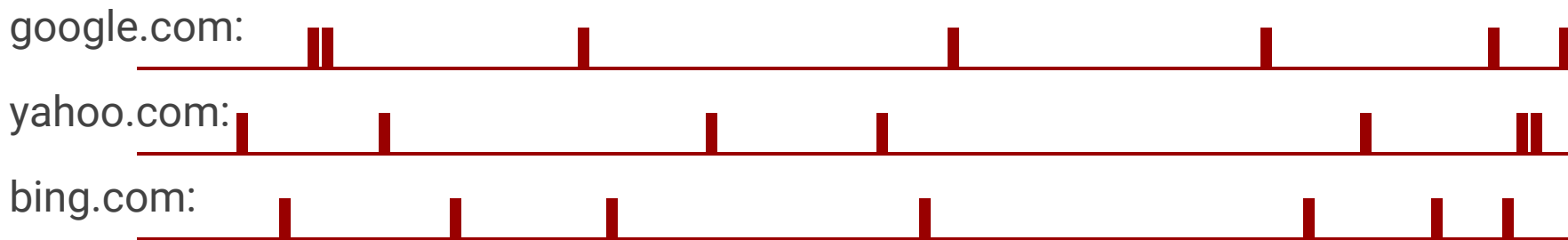


# Decoding RAPTOR

## True bit counts, with no noise



## De-noised RAPPOR reports



# From denoised counts to distribution

Linear Regression:

$$\min_X \|B - A X\|_2$$

LASSO:

$$\min_X (\|B - A X\|_2)^2 + \lambda \|X\|_1$$

Hybrid:

1. Find support of  $X$  via LASSO
2. Solve linear regression to find weights